

Fig. 2. Sample seismograms from the Tennant Creek earthquakes. For the 6 seismograms on the right the short period (solid lines) and the long period (dashed) are plotted at the same time scale and superimposed. In this figure only, seismograms have been normalized by their maximum amplitudes.

od P and SH (Figure 3) and short period P (Figure 4) waveforms were inverted simultaneously for a point-source double couple mechanism (strike, dip, and rake of the fault plane), the centroid depth, and the amplitudes of overlapping triangles representing the source time function [Nabelek 1984; McCaffrey and Abers 1988]. This method estimates the centroid double couple, which can be thought of as the weighted average of a time varying mechanism, where the

weighting factor is the seismic moment. If the fault orientation changed during rupture, the centroid mechanism will differ from that at the initiation of rupture and some first motions may be violated.

The best fitting solutions are largely thrust and, with the exception of TC1, have only a small component of strike slip motion. Despite the variation in mechanisms, the P axes inferred from them are remarkably similar for all three events; their azimuths range only from 16° to 20° (Table 1).

The waveforms constrain centroid depths to be less than 6 km, with the best matches at 3 to 4 km (Figure 3; Table 1). Attempts to place the sources deeper, for example at 9 km, near the bottom of the aftershock zone reported by Bowman et al. [1988], resulted in the solutions becoming strike slip in order to match the high amplitudes of the SH waves relative to the P waves, but the overall fit was degraded (Figure 3).

Unlike those from TC2 and TC3, the short period seismograms for TC1 are matched poorly with a point source (Figure 4, top). The match to the TC2 and TC3 short period seismograms rules out structure as the cause of the complexity in the TC1 seismograms. The compactness and high amplitudes of the HKC and SHK seismograms relative to the point source seismograms suggest that the directivity of the source for TC1 was toward these stations. A line source propagating horizontally toward the WNW produces a better fit (Figure 4; case II) than one propagating westward (case I) but greater agreement occurs when the source propagates toward the NW. A line source propagating updip along the SW dipping nodal plane (case IV) matches the short period seismograms better than

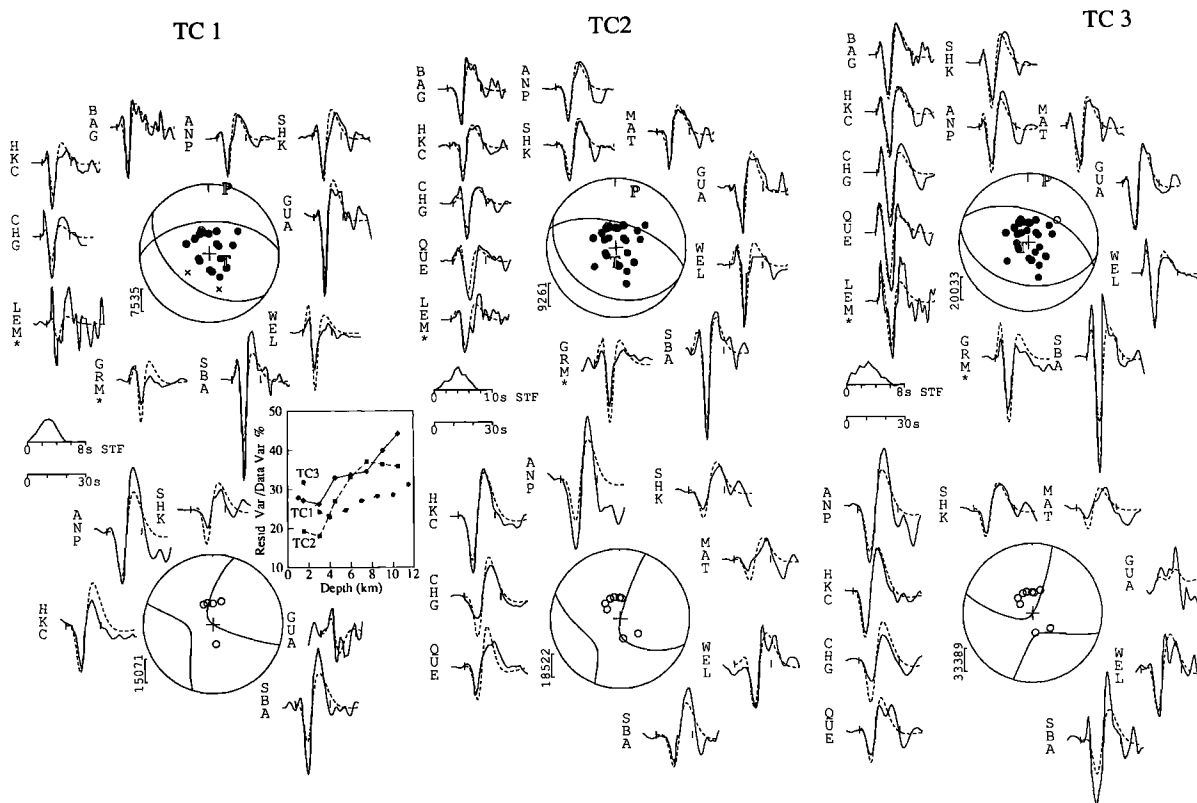


Fig. 3. Fault plane solutions for the three Tennant Creek earthquakes determined by simultaneous inversion of long and short period seismograms. At the top are the long period P waveforms and at the bottom are the SH waveforms. Short period seismograms for these mechanisms are shown in Figure 4. In the top focal sphere, dots represent compressional P wave first motions, circles are dilatations, and x's are nodal arrivals. Solid lines are observed seismograms and dashed lines are calculated. The amplitudes of the WWSSN seismograms are corrected for instrument magnification ($\times 3000$), geometrical spreading at a delta of 40° , and attenuation, but are not otherwise normalized (amplitude scales in microns are beside each focal sphere). Resulting source time functions are shown on the axes labeled STF and the other time axis is for the seismograms. Assumed values of t^* (travel time/average Q) are 1.0s for P and 4.0s for SH. Stations LEM and GRM are outside the acceptable distance range (30° to 90°) for this technique and are not used. Ticks enclose the portions of the seismograms used in the inversion. Source and receiver structures are halfspaces with $v_p=6.00$ km/s, $v_s=3.43$ km/s, and density of 2.70 g/cm 3 . The inset plot shows the variance of the residual seismogram amplitudes divided by the variance of the data for a range of depths using point sources. At each depth the waveforms were realigned to maximize fit while keeping the starting time within 1s of the arrival times on short period seismograms. The inversion was then run while all parameters except depth were allowed to change.

TABLE 1. Tennant Creek earthquake double couple point source parameters from waveform analysis

Origin Time	Duration, s	Depth, km	Moment, 10 ¹⁸ Nm	Fault Plane			Auxiliary Plane			P axis		T axis	
				Strike	Dip	Rake	Strike	Dip	Rake	Az	Pl	Az	Pl
TC1 0:35:57	4.2(0.5)	2.7(2.6)	3.66(0.26)	128(7)	45(6)	120(9)	268(11)	52(5)	63(11)	17	3	116	69
TC2 3:57:25	5.9(0.5)	3.0(1.3)	5.77(0.34)	117(6)	30(3)	100(6)	286(6)	61(3)	84(6)	20	15	182	74
TC3 12: 4:58	5.4(0.4)	4.2(1.9)	9.77(0.61)	102(8)	38(2)	82(7)	292(5)	53(2)	96(6)	18	8	230	81

Strike, dip, rake, azimuth (Az), plunge (Pl) angles are given in degrees. Estimated uncertainties are given in parentheses (likely uncertainties are 2 standard deviations for duration and moment, 10 standard deviations for depth, and 5 standard deviations for strike, dip, and rake [Nabelek 1984]).

one moving downdip along the north dipping plane (case III). This preliminary examination suggests that the fault plane for TC1 dips to the SW.

The strikes of both nodal planes for both TC2 and TC3 parallel the trend of the K and LS scarps (110°; Bowman 1988a) within the

uncertainties. The south dipping planes are certainly the fault planes. The best overall fit to the waveforms is found for TC2 but its centroid mechanism violates the first motion polarities at BAG and PMG (Figure 3). The short period first motions at HKC and BAG are of opposite polarity (Figure 2) but an inversion performed while the dip of the north dipping plane was forced to fit these first motions (i.e., dip=64°) could not produce an acceptable match to the observed long period seismograms, particularly those P waves to the NW (this trial results in a poorer match to CHG and QUE than that shown in Figure 5). Since the waveform data are sensitive to the episode of faulting in which most of the seismic moment was generated, the inconsistent first motions suggest that the mechanism changed after the onset of faulting. The inclusion of line sources for events TC2 and TC3 did not improve the fits to the waveforms over the point source models.

Relocation

Arrival times are used to calculate probability density functions [Tarantola and Valette 1982] for the relative locations of the three earthquakes using a master event technique. The *a posteriori* probability density function P for the location of the earthquake (with the origin time term removed and assuming gaussian data) is given by

$$P(X,Y,Z)=K p(X,Y,Z) \exp\{-1/2 R^T(C_t+C_m)^{-1}R\} \quad (1)$$

where K is the sum of the weights, p is an *a priori* probability density function, R is the vector of arrival time residuals with its mean removed, and C_t and C_m are the covariance matrices for the observations and the model, respectively. The errors in the observations e_t and in the model e_m are assumed to be uncorrelated so that C_t=e_t²I and C_m=e_m²I where I is the identity matrix. In our case, the source depth z_e is known independently and the *a priori* density function is p(X,Y,Z)=1 for Z=z_e, and p=0 for other depths.

The data errors e_t are assumed to be 0.5s for arrivals picked by the author from short period records, 1.5s for arrivals from long period seismograms (by cross-correlation with synthetic seismograms), and 2.0s for arrival times picked by others. Because the master event technique uses the difference between two arrival times, these errors are double the normal estimate. The master event approach also eliminates the effects of ray path differences outside the source region, so the model error e_m is that within the source region only, taken to be 0.1s.

The master event TC3 is shown near the LS fault but at a distance to the south consistent with its centroid depth and dip angle (Figure 1). This position is arbitrary but is within the 90% confidence limit for its location determined from arrival times at the Waramunga array, 30 km to the east [Bowman 1988b]. The values of P(X,Y) for the locations of events TC1 and TC2 relative to TC3 were calculated every 0.01° of latitude and longitude and contoured (Figure 1). The contours are circular indicating that the weighted observations are evenly distributed. Using TC2 as the master resulted in similar relative locations of the 3 events but a closer grouping. Because this is a relative location the position of the group of earthquakes with respect to ground features is arbitrary.

The relocated epicenters correspond to the nucleation points for the earthquakes since they are based largely on short period arrival times. Both TC1 and TC2 appear to have nucleated to the north or NW of TC3, which probably ruptured the Lake Surprise (LS) fault. Unless TC3 occurred at the far eastern end of the LS fault, which is unlikely since TC3 seismograms show no finite fault effects, then

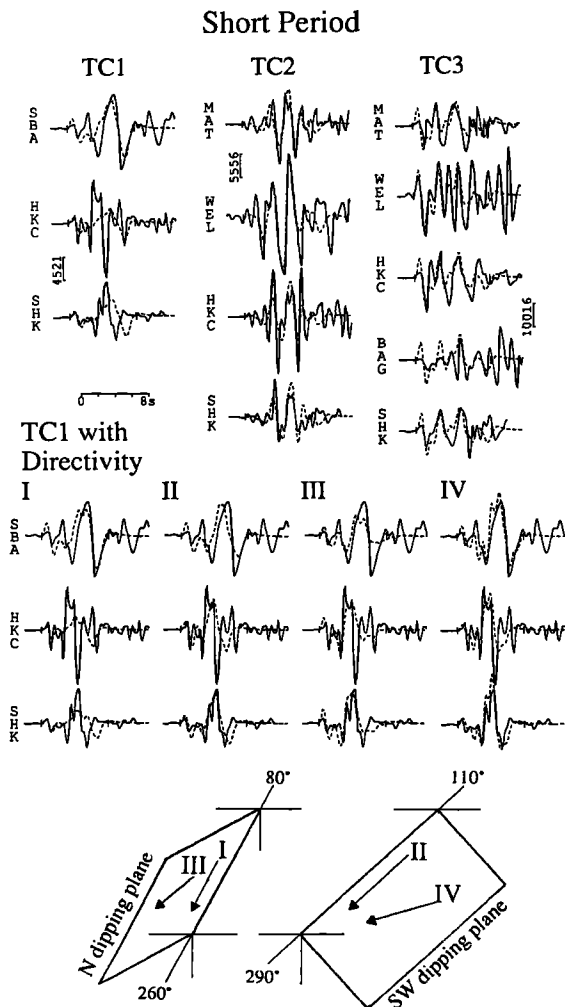


Fig. 4. (top) Observed and calculated short period seismograms for point source solutions shown in Figure 3. Amplitude scales (in microns) correspond to a WWSSN short period instrument at a distance of 40° with a magnification of 25,000. Attenuation was calculated with a t* of 0.7s. (bottom) Short period seismograms for event TC1 using propagating line sources (rupture velocity=2.5 km/s) as shown in the sketch at the bottom: (I) horizontal rupture toward azimuth of 260°; (II) horizontal rupture toward azimuth of 290°; (III) rupture toward azimuth of 330° and down the dip of the north dipping plane; and (IV) rupture toward azimuth of 330° and up the dip of the SW dipping plane. For each trial the inversion was done using all seismograms.

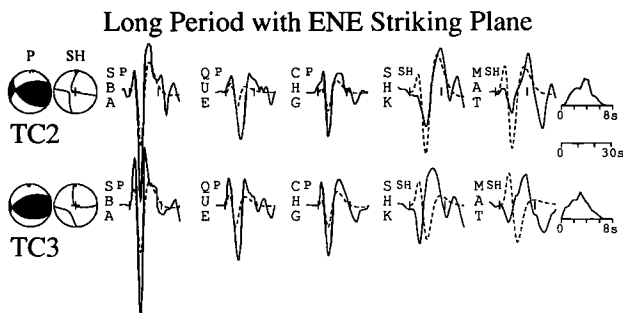


Fig. 5. Seismograms for events TC2 and TC3 showing the misfit when they have an ENE striking, NNW dipping nodal plane corresponding to the WLS fault. For this test the orientation of one nodal plane was constrained (strike= 250° , dip= 55° NW) and the best fitting values for the remaining parameters (rake angle, depth, and source time function) were determined by inversion of all seismograms.

TC1 and TC2 both started near the western end of the LS fault, as shown in Figure 1.

Discussion and Conclusions

Given the three apparently distinct segments of ground rupture and the three large earthquakes, one is first tempted to make a one-to-one correspondence. TC1 is the only one of the three events that displays a nodal plane consistent with a north dip on the WLS fault (Figures 1 and 5). The plane striking $268 \pm 7^\circ$ and dipping $52 \pm 5^\circ$ N agrees with the azimuth of the ground break (260°) and aftershocks that apparently define a zone dipping 55° N. The other nodal plane (strike= $128 \pm 7^\circ$, dip= $45 \pm 6^\circ$ S) is consistent with the trends of both the K and LS faults (110°) and the dip of the fault planes (50° S and 40° S, respectively) inferred from aftershocks. Evidence against TC1 rupturing the north dipping plane on the WLS fault is the combination of the directivity in the short period P waves, showing a northward propagating rupture, and the relocations (Figure 1 and Bowman [1988b]) that place TC1 west of the other events. If TC1 initiated in the west and ruptured westward then this event, if any, occurred on the K fault. The source duration for TC1 (4s for both the point and line sources) corresponds to a fault length of about 10 km, assuming a unilateral rupture with a velocity of 2.5 km/s, which is the distance from the inferred nucleation point for TC1 to the western end of the K scarp (Figure 1). I suggest that TC1 has more of a thrust mechanism than the best-fit solution displays (the available waveforms for TC1 cannot rule out a pure thrust mechanism) and occurred on the K fault.

For TC2, the source time function, which represents the temporal variation of the seismic moment produced by the faulting, is small for 3s, then roughly doubles for another 3s (Figure 3) indicating a sudden doubling of either the fault slip or fault area (the seismic moment is proportional to the product of the average slip and the fault area). TC2 apparently initiated beneath the unbroken region between the LS and K scarps (Figure 1) and ruptured symmetrically. I suggest that the initial 3s of the slip for TC2 was in the region of no ground breakage and that the sudden increase in moment was caused by an increase in the slip that allowed the fault to break the surface at the K or LS scarp or both.

The waveform solution for TC3 agrees closely with the field observations and aftershocks for the eastern LS fault. First, the observed trend of the fault (110°) is similar to the strike of the south dipping plane ($102 \pm 8^\circ$). Second, the dip of the fault inferred from the aftershocks is 40° S while waveforms give a dip of $38 \pm 2^\circ$ S. Third, Bowman [1988a] reports 25-30 cm of left lateral displacement on the LS fault; this is roughly 15-20% of the dip slip component and predicts a rake angle of approximately 80° , in agreement with that found here for TC3 ($82 \pm 7^\circ$). Finally, the centroid depth (4.2 ± 1.9 km) is roughly half the maximum depth of the aftershocks (9 km) reported by Bowman et al. [1988]. The estimated seismic moment for TC3 (10^{19} Nm) is comparable to that of the 1968 Meckering earthquake ($M_0 = 1.04 \pm 0.05 \times 10^{19}$ Nm [Frederich et al. 1988]). This moment predicts an average slip of 1.8m on the LS fault (using a fault length of 12 km and down-dip width of $9 \text{ km} / \sin(38^\circ) = 15 \text{ km}$) which is similar to that observed at the surface.

The apparent anomaly in the Tennant Creek earthquake se-

quence is the WLS scarp. Evidently it displays north-side-up displacement and has been interpreted as the surface expression of a north dipping thrust fault on the basis of aftershock locations [Bowman et al. 1988]. If so it requires an extremely complex geometry since the K and LS faults dip to the south. As explained above, it is unlikely that any of the three largest January 22 events occurred on such a north dipping thrust fault. At this time, I am disinclined to reject the teleseismic constraints on the basis of unpublished aftershock locations, which are often difficult to interpret, and may not reveal faults that were active during the main faulting episode.

Alternatively, the WLS scarp may represent coseismic or postseismic failure of the hanging wall. Extensive normal faults with throws of several meters were observed in the hanging wall of the 1980 El Asnam earthquake, particularly in the north where only normal faulting was seen at the surface yet geodetic and seismologic data demonstrated that thrust faulting was the dominant mode of deformation [e.g., Nabelek 1985]. If dip slip faulting at the WLS fault was contained within the hanging wall, its seismic moment would be at most 1.3×10^{18} Nm for an average 1m of slip; an earthquake of this size is below the noise level of TC2 and TC3. Recall that short period first motions at stations to the NW for TC2 are consistent with a nodal plane dipping steeply to the NW and not with the centroid solution; perhaps the WLS fault ruptured at the beginning of TC2 but its signal was obscured by a much larger event that followed quickly on a SW dipping fault.

The WLS fault coincides with a quartz ridge; these are known to mark faults in the Proterozoic rocks of NE Australia [Bowman 1988b]. I suggest that the the Kunayungku and Lake Surprise scarps represent the same SW dipping fault in the crust and that all three of the large earthquakes occurred on this fault. The West Lake Surprise fault, a pre-existing weak zone in the hanging wall, created a discontinuity in stress on the fault surface at its intersection with the fault plane. This discontinuity inhibited slip from continuing from the Kunayungku section to the Lake Surprise section, causing multiple events rather than a single large earthquake, which to now has typified large Australian events.

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